

**Supporting Table S 1: List of features defined for all tuning curves.**  
Each feature is calculated once for uni, once for afix and once for ain condition.

Feature name	Description
GLOBALMINIMUMANGLE <sup>a</sup>	$\operatorname{argmin} tc(\theta)$
GLOBALMINIMUM	$\min tc(\theta)$
GLOBALMAXIMUMANGLE	$\operatorname{argmax} tc(\theta)$
GLOBALMAXIMUM	$\max tc(\theta)$
PEAKTOPEAK <sup>b</sup>	GLOBALMAXIMUM - GLOBALMINIMUM
INNERMINIMUMANGLE <sup>c</sup>	$\operatorname{argmin}_{\theta \in I} tc(\theta)$
INNERMINIMUM	$tc(\operatorname{INNERMINIMUMANGLE})$
OUTERMINIMUMANGLE <sup>d</sup>	$\operatorname{argmin}_{\theta \in O} tc(\theta)$
MAXIMUMANGLE <sup>right e</sup>	$\operatorname{argmax}_{\theta \in R} tc(\theta)$
INNERWIDTH <sup>right</sup>	$(\operatorname{MAXIMUMANGLE}^{\text{right}} - \operatorname{INNERMINIMUMANGLE}) \bmod 360$
OUTERWIDTH <sup>right</sup>	$(\operatorname{OUTERMINIMUMANGLE} - \operatorname{MAXIMUMANGLE}^{\text{right}}) \bmod 360$
WIDTH <sup>right</sup>	$\operatorname{INNERWIDTH}^{\text{right}} + \operatorname{OUTERWIDTH}^{\text{right}}$
$\Delta$ WIDTH <sup>right</sup>	$\operatorname{OUTERWIDTH}^{\text{right}} - \operatorname{INNERWIDTH}^{\text{right}}$
MAXIMUM <sup>right</sup>	$tc(\operatorname{MAXIMUMANGLE}^{\text{right}})$
PEAKTOPEAK <sup>right</sup>	$tc(\operatorname{MAXIMUMANGLE}^{\text{right}}) - \operatorname{GLOBALMINIMUM}$
SKEWNESS <sup>right fg</sup>	$\operatorname{mom}_3(\tilde{R}) / \operatorname{mom}_2^{1.5}(\tilde{R})$
KURTOSIS <sup>right</sup>	$\operatorname{mom}_4(\tilde{R}) / \operatorname{mom}_2^2(\tilde{R})$
DIP <sup>right</sup>	$\operatorname{MAXIMUM}^{\text{right}} - \operatorname{INNERMINIMUM}$
INNERBANDWIDTH <sub>X%</sub> <sup>right h</sup>	$bw(\operatorname{MAXIMUMANGLE}^{\text{right}}, \text{left}, X)$
OUTERBANDWIDTH <sub>X%</sub> <sup>right</sup>	$bw(\operatorname{MAXIMUMANGLE}^{\text{right}}, \text{right}, X)$
BANDWIDTH <sub>X%</sub> <sup>right</sup>	$\operatorname{INNERBANDWIDTH}_{X\%}^{\text{right}} + \operatorname{OUTERBANDWIDTH}_{X\%}^{\text{right}}$
TC SYMMETRY INDEX	$\sqrt{\sum_{\theta} (tc(\theta) - tc(360 - \theta))^2 / 2}$

<sup>a</sup>The value of this circular variable was chosen to lie in the range  $[-120^\circ, 240^\circ)$

<sup>b</sup>if PEAKTOPEAK  $< 10^{-10}$  don't calculate any feature at all

<sup>c</sup> $I = [0, 360)$  for uni conditions; for afix and ain first find local maxima for  $45 \leq \theta \leq 315$  (to avoid spurious local maxima require that there's no higher point in the tuning curve within  $15^\circ$  on both sides of the local maxima). If there's no such local maximum  $I = (120, 240)$ , if there's one at  $180^\circ$   $I = (120, 240)$ ; if there's one at  $\theta_m \neq 180^\circ$   $I = (\theta_m, 240)$  or  $I = (120, \theta_m)$  depending on if  $\theta_m$  lower or greater than  $180^\circ$ ; if there are two  $I = (\theta_0, \theta_{-1})$  where  $0 \leq \theta_0$  and  $\theta_{-1} \leq 360$  are the local maxima closest to  $0^\circ$  and  $360^\circ$ ; if there are more than two: if all of them are  $\leq$  or  $\geq 180^\circ$  also use  $I = (\theta_0, \theta_{-1})$ , otherwise there's at least one to the left and at least one to the right of  $180^\circ$ ; pick the highest on either side; if, in addition, there is a local maximum at  $180^\circ$ , calculate it's distance  $d$  to the left and right peak according to  $((x_{\text{left/right}} - x_{180})/360)^2 + ((y_{\text{left/right}} - y_{180})/\text{ptp})^2$ ; replace the peak which is closer according to the measure  $d$  if the peak at  $180^\circ$  is higher than it

<sup>d</sup> $O = [0, 360)$  for uni conditions; for afix and ain  $O = [0, 360) \setminus I$

<sup>e</sup> $R = [180, 300]$  for uni conditions; for afix and ain  $R = [\operatorname{INNERMINIMUMANGLE}, 315]$ ; if  $tc(\operatorname{MAXIMUMANGLE}^{\text{right}}) = \operatorname{GLOBALMINIMUM}$  then  $\operatorname{MAXIMUMANGLE}^{\text{right}}$  (and likewise all dependent features) is not defined

<sup>f</sup> $\operatorname{mom}_n(X) = \sum_{x \in X} (x - \bar{X})^n / n$  and  $\bar{X}$  is the mean of set  $X$

<sup>g</sup>if  $0 \leq \operatorname{INNERMINIMUMANGLE} < \operatorname{OUTERMINIMUMANGLE} \leq 360$  then  $\tilde{R} = [\operatorname{INNERMINIMUMANGLE}, \operatorname{OUTERMINIMUMANGLE}]$ , otherwise  $\tilde{R} = [0, 360) \setminus [\operatorname{OUTERMINIMUMANGLE}, \operatorname{INNERMINIMUMANGLE}]$

<sup>h</sup> $bw(m, d, X)$  is defined as follows given the tuning curve  $tc$ : starting from position  $m$  it returns the first angle  $\theta$  in direction  $d \in \{\text{left}, \text{right}\}$  for which  $tc(\theta) < \frac{X}{100} \operatorname{PEAKTOPEAK}$ . Additionally, if an inner bandwidths (denoted "I") calculated this way is greater than the distance  $d$  of the corresponding peak to  $\operatorname{INNERMINIMUMANGLE}$ , the bandwidth is set to  $d$