

CORRECTION

Correction: Several supplementary concepts for applied category-theoretical states over an extended Petri net using an example relating to genetic coding: Toward an abstract algebraic formulation of molecular/genetic biology

Jitsuki Sawamura, Shigeru Morishita, Jun Ishigooka

In the Firing rules: For a morphism (transition), there are two types of firing rules labeled I and II subsection of the Methods, there is an error in the first sentence of the 12th paragraph. The correct sentence is: Similarly, the following relation may arise,

$$\{a_{(k)i}\}; (f_{(k)a}; f_{(k)b}); f_{(k \rightarrow m)} = \{a_{(k)i}\}; f_{(k)a}; (f_{(k)b}; f_{(k \rightarrow l)}) = a_{(l)s}(\text{group } A_l) \quad (9)$$

(r, s ; appropriate non-negative integers that provide adequate elements).

In the Marking of a PN as an optional display subsection of the Methods, there is an error in 12th and 16th equation. Please view the complete, correct equation here.

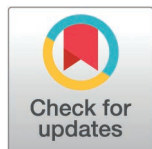
$$S_w = \{a_{(1)2}, a_{(1)3}, \dots\} p_1 \oplus \{ \dots, a_{(2)3}, \dots\} p_2 \oplus \{\phi\} p_3 \oplus \dots \oplus \{ \dots, a_{(k)i}, a_{(k)j}, \dots\} p_k \oplus \dots \oplus \{a_{(m)2}, a_{(m)5}, \dots\} p_m \parallel \{\phi\} p_{m+1} \oplus \{\phi\} p_{m+2} \oplus \dots \quad (12)$$

$$S_i = \{a_{(1)0}\} p_1 \oplus \{a_{(2)0}\} p_2 \oplus \dots \oplus \{a_{(k)0}\} p_k \oplus \dots \oplus \{a_{(m)0}\} p_m \parallel \{\phi\} p_{m+1} \oplus \{\phi\} p_{m+2} \oplus \dots \quad (16)$$

In the An explicit/implicit identity protein and its treatment subsection of the An example of composition in the DNA model, there is an error in the 12th sentence of the third paragraph. The correct sentences is: Moreover, $\langle Pr_{(k)0} \rangle$ is defined as the state where the ‘ Δ ’s of the explicit identity protein are deleted via the annihilation morphism for $Pr_{(k)0}$; ‘ $\{Pr_{(k)0}\}; f_{(k \rightarrow \phi)} = \langle Pr_{(k)0} \rangle; f_{(k \rightarrow \phi)} = [\Delta_0 | \Delta_1 \Delta_2 \Delta_3 \dots]; f_{(k \rightarrow \phi)} = [()()()] = \phi \phi \phi \dots \phi = \phi = Pr_{\phi}$ ’ (in this instance, $k = 6$).

In the An explicit/implicit identity protein and its treatment subsection of the An example of composition in the DNA model, there is an error in the 15th sentence of the third paragraph. The correct sentence is: Naturally, an inverse procedure is considered via the creation morphism, ‘ $\{\phi\}; f_{(\phi \rightarrow k)} = \{Pr_{\phi}\}; f_{(\phi \rightarrow k)} = Pr_{(k)0} = \langle Pr_{(k)0} \rangle = \Delta \Delta \Delta \dots \Delta$ ’ (with $k = 6$).

In the Regarding the symbols $[[]]$, $()$ and $\langle \rangle$ that treat the explicit/implicit deletion of identity elements subsection of the An example of composition in the DNA model, there is an error in the third sentence of the second paragraph. The correct sentence is: In the above example, by performing the additional operation $\langle \rangle_{13, \infty}$ to $Rs_{(4)2}$, $((Rs_{(4)2}^{\dagger}; \langle \rangle_{4,6}; \langle \rangle_{10,12}; \langle \rangle_{16,18})); \langle \rangle_{13, \infty} = [E_0 | A_1 U_2 G_3 C_4 U_5 G_6 C_7 G_8 U_9 A_{10} C_{11} G_{12} | E_{13} E_{14} E_{15} \dots] = \langle Rs_{(4)2}^{\dagger} \rangle$ (in place p_5).



OPEN ACCESS

Citation: Sawamura J, Morishita S, Ishigooka J (2025) Correction: Several supplementary concepts for applied category-theoretical states over an extended Petri net using an example relating to genetic coding: Toward an abstract algebraic formulation of molecular/genetic biology. PLoS ONE 20(4): e0322567. <https://doi.org/10.1371/journal.pone.0322567>

Published: April 17, 2025

Copyright: © 2025 Sawamura et al. This is an open access article distributed under the terms of the [Creative Commons Attribution License](https://creativecommons.org/licenses/by/4.0/), which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

In the Regarding the symbols $[[[]]$, $(([]))$ and $\langle\langle\rangle\rangle$ that treat the explicit/implicit deletion of identity elements subsection of the An example of composition in the DNA model, there is an error in the fifth and sixth sentences of the second paragraph. The correct sentences are: In an ordinal $\langle\text{Rs}_{(4)2}\rangle$, $s = 1$, $r = \infty$ is imposed, and $\langle\text{Rs}_{(4)2}\rangle = \langle\text{Rs}_{(4)2}\rangle_{1,\infty} = [E_0|A_1U_2G_3C_4U_5G_6C_7G_8U_9A_{10}C_{11}G_{12}||E_{13}E_{14}E_{15}\dots]$ (in place p_5). For the ‘part of the operation f_{t-sp} ($=f_{(4\rightarrow6)}$) and $f_{post-prot}$ ($=f_{po-pr}=f_{(6\rightarrow7)}$); we see $f_{(4\rightarrow6)}$; $f_{(6\rightarrow7)}$ and $f_{(4\rightarrow5)}$; $f_{(5\rightarrow7)}$ commute because all tokens of place p_5 are products of $\text{Rs}_{(4)2}^\dagger; \langle\langle\rangle\rangle_{r,s}; \dots$ to a sequence of amino acids (protein) (in place p_6) from the r -th to the s -th coordinate (s, r : non-negative integers with $s \leq r$; $s, r = 0, 1, 2, \dots$) of, say, token $\text{Rs}_{(4)2}^\dagger$, denoted ‘ $\langle\text{Rs}_{(4)2}^\dagger; []_{s,r}$ ’, the following manipulation is verified for ‘ $\text{Rs}_{(4)2}^\dagger = [E_0|A_1U_2G_3O_{4-6}C_7U_8G_9O_{10-12}C_{13}G_{14}U_{15}O_{16-18}A_{19}C_{20}G_{21}||E_{22}E_{23}E_{24}\dots]$ (in place p_5)’.

$$\langle\text{Rs}_{(4)2}^\dagger; []_{7,9}\rangle = [E_0|A_1U_2G_3O_{4-6}L_{7-9}O_{10-12}C_{13}G_{14}U_{15}O_{16-18}A_{19}C_{20}G_{21}||E_{22}E_{23}E_{24}\dots]. \quad (46)$$

In the Regarding the symbols $[[[]]$, $(([]))$ and $\langle\langle\rangle\rangle$ that treat the explicit/implicit deletion of identity elements subsection of the An example of composition in the DNA model, there is an error in the first sentence of the eighth paragraph. The correct sentence is: Similarly, for morphism f_{po-pr} ($=f_{(6\rightarrow7)}$); if the deletion of explicit ‘ Δ ’s from the r -th to the s -th coordinate (s, r : non-negative integers with $s \leq r$; $s, r = 0, 1, 2, \dots$) of, say, token ‘ $\text{Pr}_{(6)2}$ ’ is denoted ‘ $\text{Pr}_{(6)2}; \langle\langle\rangle\rangle_{s,r}$ ’, the following manipulation is verified for ‘ $\text{Pr}_{(6)2} = [\Delta_0|M_1\Delta_2\Delta_3\Delta_4L_5R_6\Delta_7\Delta_8T_9R_{10}\Delta_{11}\Delta_{12}L_{13}M_{14}||\Delta_{15}\Delta_{16}\Delta_{17}\dots]$ (in place p_6)’.

$$\text{Pr}_{(6)2}; \langle\langle\rangle\rangle_{2,3} = [\Delta_0|M_1O_{2-3}L_4R_5\Delta_6\Delta_7\Delta_8T_9R_{10}\Delta_{11}\Delta_{12}L_{13}M_{14}||\Delta_{15}\Delta_{16}\Delta_{17}\dots].$$

In this way, $\text{Pr}_{(6)2}; \langle\langle\rangle\rangle_{2,3}; \langle\langle\rangle\rangle_{6,8}; \langle\langle\rangle\rangle_{11,12} = [\Delta_0|M_1O_{2-3}L_4R_5O_{6-8}T_9R_{10}\Delta_{11}\Delta_{12}L_{13}M_{14}||\Delta_{15}\Delta_{16}\Delta_{17}\dots]$. Then,

$$\begin{aligned} & \left(\left(\text{Pr}_{(6)2}; \langle\langle\rangle\rangle_{2,3}; \langle\langle\rangle\rangle_{6,8}; \langle\langle\rangle\rangle_{11,12} \right); \langle\langle\rangle\rangle_{15,\infty} \right) \\ &= [\Delta_0|M_1O_{2-3}L_4R_5O_{6-8}T_9R_{10}O_{11-12}L_{13}M_{14}||O_{15}O_{16}O_{17}\dots] \\ &= \Delta_0(M_1)(L_2)(R_3)(T_4)(R_5)(L_6)(M_7) \text{ (in place } p_7). \end{aligned} \quad (49)$$

In the A treatment of the somatic recombination (VDJ recombination) for antibodies using the concept of colimit subsection of the An example of composition in the DNA model, there is an error in the fifth sentence of the third paragraph. The correct sentence is: Hence, as an example, we have

$$J_2 = [A_1|C_2|\dots|G_{N_j}||E_{(N_j+1)}|E_{(N_j+2)}|E_{(N_j+3)}|\dots] = [A_1|C_2|T_3|G_4|A_5||E_6|E_7|E_8|\dots],$$

where the number of recognized bases is ‘ $N_j=5$ ’.

In the Discussion section, there is an error in first sentence of the ninth paragraph. The correct sentence is: Finally, the use of unit ‘1’ in Descartes’s geometry may be one of the first applications of the binary operation of group where ‘ $n;n;n;\dots;n=n;n=n$ ’ and ‘ $n=n;n=n;n;n;\dots;n$ ’ are demonstrated multiple times so that the formula ‘ $a^3+2ab+3a/b^2$ ’ is adapted entirely in three dimensions as ‘ $a^3+2ab\cdot 1+3(a/b^2)\cdot 1^4$ ’.

The Supporting Information files are incorrect. Please see the correct [S1 File](#) and [S1 Appendix](#) below.

Supporting information

S1 File. Citations for reference files are displayed.
(PDF)

S1 Appendix.
(DOCX)

Reference

1. Sawamura J, Morishita S, Ishigooka J. Several supplementary concepts for applied category-theoretical states over an extended Petri net using an example relating to genetic coding: Toward an abstract algebraic formulation of molecular/genetic biology. PLoS One. 2024;19(6):e0302710. <https://doi.org/10.1371/journal.pone.0302710> PMID: [38848321](https://pubmed.ncbi.nlm.nih.gov/38848321/)