Evolutionary dynamics of an epigenetic switch in a fluctuating environment
S1 Appendix. Supplementary Table: Previous Work

| Authors | Year | Evolutionary strategies | Comparison method | Analytical/ Numerical | Phenotypes | Environment | Fitness | Selection | Explicit cost | Population size | Generations | Comments |
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| Jablonka et al. | 1995 | Inducible switching; stochastic switching | Average growth rate | Both | 2-discrete | Periodic \& random; asymmetric (2 states) | Symmetric | Differential growth rate | Induction delay | Growing (discrete) | Nonoverlapping | They compared three different strategies: non-inducible (with a small stochastic transition rate), completely inducible, or an intermediate response (memory), considering some induction delay and the phenotypic memory as a tunable property. They observed that the intermediate response is advantageous under random environmental fluctuations; if the environment is strictly periodic, the inducible system is favored unless fluctuations occur faster than the induction delay. |
| Lachmann \& Jablonka | 1996 | Inducible switching; stochastic switching | Average growth rate | Analytical | 2-discrete | Periodic (2 states) | Symmetric | Differential growth rate | None | Growing (discrete) | Nonoverlapping | They explored the optimal values for the transition rates under fluctuating environments; they concluded that for noninducible systems, the optimal rate for random transitions is around the frequency of the environmental fluctuations. |
| Thattai \& van Oudenaarden | 2004 | Inducible switching; stochastic switching | Average growth rate | Analytical | 2-discrete | Periodic \& random (2 states) | Symmetric | Differential growth rate | None | Growing (continuous) | Continuous time (ODEs) | They considered that the transitions between phenotypic states depend on the environment and explored under which circumstances a transition rate to the "unfit" state different to zero will be selected; they concluded that if the transition to the "fit" state is fast enough -short induction delay-, an homogeneous population will be always favored. |
| Kussell \& Leibler | 2005 | Inducible switching; stochastic switching | Average growth rate | Analytical | $n$-discrete | Random ( $n$ states) | No explicit assumption | Differential growth rate | Sensing, diversity \& induction delay costs | Growing (continuous) | Continuous time (ODEs) | They compared inducible to stochastic transitions but taking in account the cost of sensing, the induction delay and the diversity cost imposed by the stochastic switching. They concluded that a sensor is only worth if the environment is highly uncertain, and the stochastic switching will be favored when the environment changes infrequently. |
| Kussell et al. | 2005 | Stochastic switching | Average growth rate | Both | 2-discrete | Periodic; asymmetric (2 states) | Asymmetric | Differential growth rate | None | Growing (continuous) | Continuous time (ODEs) | They considered only stochastic transitions, and they observed that the type of environmental changes determines the strategy to be used. |
| Wolf et al. | 2005 | Fixed; inducible switching; stochastic switching | Average growth rate | Both | $n$-discrete (focus on $n=2$ ) | Random; asymmetric ( $n$ states) | Asymmetric | Differential growth rate | None | Growing (discrete) | Nonoverlapping | They considered more flexible adaptation strategies, going from ignoring the environment, a deterministic inducible response, stochastic inducible response, to pure stochastic switching. If no sensor exists, stochastic switching is always selected under the time-varying environmental conditions selected here, as well as if the detection of the sensor is bad or long induction delays exist. |
| Ribeiro | 2008 | Inducible; stochastic switching (bistable genetic circuit) | Invasion | Simulations | Continuous (mechanistic) | Random (2 states) | Symmetric | Truncation selection | None | $\begin{aligned} & \text { Fixed (discrete; } \\ & 1000 \\ & \text { individuals) } \end{aligned}$ | Nonoverlapping | He modeled individual cells as toggle switches and explored the population behavior under a fluctuating environment, considering both inducible systems and pure stochastic switching. He concluded that the optimal noise level depends on the environmental fluctuations, and as noise increases, the fitness increases too in fast fluctuating environments. |
| Salathé et al. | 2009 | Fixed; stochastic switching | Invasion | Simulations | 2-discrete (x 2-modifier states) | Periodic \& random (2 states) | Asymmetric | Proportional selection scheme | None | Infinite (subpopulation frequencies) | Nonoverlapping | Assuming an infinite population and following subpopulation frequencies through generations, they explored the impact of asymmetric fitness landscapes. They concluded that with the fitness asymmetry over a certain threshold, unless the selection pressure is very strong in both environments, ignoring the environment becomes optimal over stochastic switching (with an optimal rate approximately equal to the environmental fluctuation frequency). |
| Gaál et al. | 2010 | Fixed; stochastic switching | Average growth rate | Analytical | 2-discrete | Periodic; asymmetric (2 states) | Asymmetric | Differential growth rate | None | Infinite (subpopulation frequencies) | Continuous time (ODEs) | They observed that as the asymmetry in the environments increases, the selected strategy goes from the optimal stochastic switching population (where the transition rate is assumed equal in both directions) to an equally optimal nonswitching and switching populations, to finally being optimal to ignore the environment, even if a local maximum still exists for a switching rate distinct to zero. |


| Visco et al. | 2010 | Fixed; stochastic switching | Average growth rate | Analytical | 2-discrete | Responsive (i.e. catastrophe rate depends on the population); random (one normal state \& instantaneous catastrophe) | Asymmetric | Differential growth rate | None | Growing (continuous) | Continuous time (ODEs) | They explored the selection of stochastic switching under a single environment with occasional and instantaneous catastrophic events whose rate depends on the population structure. They observed that stochastic switching strategy is favored by strong catastrophes, while non-switching by weak catastrophes. |
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| Liberman et al. | 2011 | Stochastic switching | Average growth rate \& invasion | Both | 2-discrete (x2-modifier states with recombina- tion) | Periodic (2 states) | Symmetric | Differential growth rate | None | Infinite (subpopulation frequencies) | Nonoverlapping | They took Salathé et al. (2009) and Gaál et al. (2010) one step forward including recombination in the model; they observed that, under their model, recombination makes unlikely that a stable non-zero transition rate exists. |
| Libby \& Rainey | 2011 | Fixed; stochastic switching | Average probability of being selected | Both | 4-discrete | Periodic (one normal state \& instantaneous catastrophe) | Symmetric | Strong frequency dependent selection: exclusion rule + bottleneck | $\begin{aligned} & \text { Switching } \\ & \text { cost } \end{aligned}$ | Growing (continuous) | Continuous time (ODEs) | They considered a strong frequency-dependent selection, with an exclusion rule for the most fitted subpopulation and bottleneck when the environment changes. Even considering <br> a switching cost-reducing the growth rate on switching genotypes-, exclusion rules are observed to favor switching phenotypes; on the other hand, larger (weaker) bottlenecks permit faster-growing, non-switching types to pass through to the next "round" outgrowing the switching type. |
| Carja \& Feldman | 2012 | Stochastic switching | Probability of survival | Simulations | $n$-discrete | Periodic (2 states) | Symmetric | Proportional selection scheme | None | $\begin{aligned} & \text { Fixed (discrete; } \\ & 10000 \\ & \text { individuals) } \end{aligned}$ | Nonoverlapping | They found that phenotypic variability increases in populations under fast fluctuating environments, but this effect disappears as the fluctuations become less frequent. |
| Kuwahara \& Soyer | 2012 | Genetic adaptation; stochastic switching (bistable genetic circuit) | Natural selection | Simulations | Continuous (mechanistic) | Periodic \& random (2 states) | Symmetric (binary function) | Proportional selection scheme | None | $\begin{gathered} \text { Fixed (discrete; } \\ 1000 \\ \text { individuals) } \end{gathered}$ | Nonoverlapping | They not only included a mechanistic model, but considered the genetic adaptation to explore the adaptive origin of stochastic epigenetic switches under fluctuating environments. They observed that bistability emerges and is maintained only in a limited range of evolutionary conditions, and suggested that its selection occurs only as a byproduct of the selection for evolvability. Noteworthy, they assumed a "binary" fitness function which would not favor the underlying bimodal distribution in a bistable system. |
| Carja et al. | 2013 | Stochastic switching | Invasion | Both | 4-discrete (x2-modifier states with recombina- tion) | Periodic \& random ( $n$ states) | No explicit assumption | Differential growth rate | None | Infinite (subpopulation frequencies) | Nonoverlapping | An extension of Liberman et al. (2011) model; they reached similar conclusions. |
| Furrow \& Feldman | 2014 | Inducible switching; stochastic switching | Invasion | Simulations | 2-discrete (x 2-modifier states with 2 epigenetic states) | Periodic \& random (2 states) | Asymmetric | Differential growth rate | Epigenetic regulation | Infinite (subpopulation frequencies) | Nonoverlapping | They expanded the classical modifier model (e.g. Salathé et al., 2009) to consider inducible switching and the associated cost. They observed that the environmental fluctuation frequency influences the conditions for evolution of epigenetic regulation (either induced or stochastic switching). |
| Carja et al. (Genetics) | 2014 | Stochastic switching | Invasion | Both | 2-discrete (x 2-modifier states with recombination) | Periodic (2 states) | Symmetric | Differential growth rate | None | Infinite (subpopulation frequencies) | Nonoverlapping | They took Salathé et al. (2009) one step forward including migration in the model, and study the evolution of switching rates in the presence of both spatial and temporal heterogeneity in selection pressures. They observed that the evolutionary dynamics of the system are mainly governed by the environmental fluctuation rate. |
| Carja et al. (PNAS) | 2014 | Stochastic switching | Invasion | Both | 4-discrete (x 2-modifier states with recombination) | Periodic \& random (2 states) | Asymmetric | Differential growth rate | None | Infinite (subpopulation frequencies) | Nonoverlapping | They took Salathé et al. (2009) and Liberman et al. (2011) one step forward including migration in the model, and compare it to the effect of mutation and recombination as sources of phenotypic variation; they observed that, under their model, these three essentially different evolutionary forces respond very similar to fluctuating selection. |


| Botero et al. | 2015 | Inducible switching; genetic adaptation | Natural selection | Simulations | Continuous | Periodic (continuous) | Symmetric | Proportional selection scheme | Phenotypic plasticity | $\begin{aligned} & \text { Fixed (discrete; } \\ & 5000 \\ & \text { individuals) } \end{aligned}$ | Nonoverlapping | They used an abstract model which, while simple, can still display plasticity, bet-hedging, and genetic adaptation. Testing multiple environmental variation patterns, they observed that different adaptive responses consistently evolve under different timescales and predictabilities of the environmental variation. |
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| Lin et al. | 2015 | Fixed; stochastic switching | Frequency | Simulations | 2-discrete | Periodic (2 states) + bottlenecks | Symmetric | Differential growth rate | None | Growing (discrete) | Continuous time | They explored the origin of the stochastic transitions in fluctuating environments distinguishing between standing variation and de novo mutations using both an experimental and a mathematical model. They concluded that the contribution of each of these mechanisms on the adaptation process depends on the fluctuation timescales. |
| Belete \& Balázsi | 2015 | Stochastic switching | Average growth rate | Both | 2-discrete | Periodic; asymmetric (2 states) | Asymmetric | Differential growth rate | None | $\begin{gathered} \text { Fixed (discrete; } \\ 10000 \\ \text { individuals) } \end{gathered}$ | Nonoverlapping | They explored the stochastic switching rate dependency to the environmental fluctuation frequency in asymmetric environments and fitness as the environmental duration shorten. In this limit, they observed that the previously described optimal switching rate matching environmental fluctuation frequency does not always hold. |
| GómezSchiavon \& Buchler | - | Genetic adaptation; stochastic switching (bistable genetic circuit) | Natural selection | Simulations | Continuous (mechanistic) | Periodic \& random (2 states) | Symmetric (Lorentzian function) | Tournament selection scheme | None | $\begin{aligned} & \text { Fixed (discrete, } \\ & 1000 \\ & \text { individuals) } \end{aligned}$ | Nonoverlapping | - |

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