

Importance sampling algorithm

Data: $y^{r, s_{\text{curr}}}$, the wILI observations so far; $z^{r, s_{\text{curr}}}$, a version of $y^{r, s_{\text{curr}}}$ with two extra points estimated from GFT; prior distributions of wILI curves, noise levels, and transformations

Result: weighted collection of curves

Let $\phi(x; \mu, \sigma)$ be the normal pdf;

for a large number of times **do**

 Randomly draw f^r , σ , ν , θ , and μ from the corresponding priors;

 Let $f^{r, s_{\text{curr}}}(i) = f_4^r(i) = b^r + \frac{\theta^r - b^r}{\max_j f^r(j) - b^r} \left[f^r \left(\frac{i - \mu^r}{\nu^r} + \arg \max_j f^r(j) \right) - b^r \right]$;

 Calculate weight $w = \prod_{i=1}^{\text{length}(z^{r, s_{\text{curr}}})} \phi(z; f^{r, s_{\text{curr}}}(i), \sigma)$;

 Let v be a 53-length vector, a possible curve for this season;

for i in $1..\text{length}(y^{r, s_{\text{curr}}})$ **do**

$v_i := y_i^{r, s_{\text{curr}}}$;

end

for i in $(\text{length}(y^{r, s_{\text{curr}}}) + 1)..53$ **do**

$v_i := f^{r, s_{\text{curr}}}(i)$;

end

 Add curve v with weight w to the collection of possibilities for this season (the posterior estimate)

end

Algorithm 1: Importance sampling procedure

Note that, since the GFT estimates are not exact, we weight $f^{r, s_{\text{curr}}}$ based on $z^{r, s_{\text{curr}}}$, using both ILINet wILI observations and GFT data, but we construct each possible curve v using $f^{r, s_{\text{curr}}}$ and $y^{r, s_{\text{curr}}}$, using no GFT. However, since ILINet data can undergo revisions, we have also considered versions that construct each v ignoring some of the more recent values in $y^{r, s_{\text{curr}}}$.

To improve computational efficiency, we also use a modified version of the code above that first divides up the possible values of f^r , σ , ν , θ , and μ into bins and estimates the average weight of $f^{r, s_{\text{curr}}}$'s in each bin. By sampling values of f^r , σ , ν , θ , and μ more frequently from the higher-weighted bins (and correcting for this decision in the weight calculation), we are able to construct a collection of curves with a high total weight more quickly than the version above.