I. DERIVATIONS OF THE THEORETICAL RESULTS

Here we give the complete derivations of the theoretical results. The following calculations are based on standard textbooks related to polymer dynamics [S1] and statistical physics [S2]. The mean-squared displacement (MSD) of the Rouse polymer in the viscoelastic environment was first analyzed by Weber et al. [S3], whose work is a useful reference for the now in the following calculations.

A. The fluctuation-dissipation relation between $g_p(t)$ and $\gamma(t)$

According to the fluctuation-dissipation relation (FDR) for $g(n, t)$,

$$
\langle g_n(n, t)g_{m}(m, t') \rangle = k_B T \gamma(t-t') \delta(n-m) \delta_{n\lambda},
$$

(S1)

the following calculations can be made:

$$
\langle g_{pn}(t)g_{q\lambda}(t') \rangle = \frac{1}{N^2} \int_0^N dn \int_0^N dm \cos \left( \frac{p\pi n}{N} \right) \cos \left( \frac{q\pi m}{N} \right) \langle g_n(n, t)g_{\lambda}(m, t') \rangle,
$$

$$
= \frac{1}{N^2} \int_0^N dn \int_0^N dm \cos \left( \frac{p\pi n}{N} \right) \cos \left( \frac{q\pi m}{N} \right) k_B T \gamma(t-t') \delta(n-m) \delta_{n\lambda},
$$

$$
= \frac{k_B T}{N} \gamma(t-t') \delta_{n\lambda} \frac{1}{N} \int_0^N dn \cos \left( \frac{p\pi n}{N} \right) \cos \left( \frac{q\pi n}{N} \right),
$$

$$
= \frac{k_B T}{N} \gamma(t-t') \delta_{n\lambda} \frac{1}{2N} \int_0^N dn \left[ \cos \left( \frac{(p-q)\pi n}{N} \right) + \cos \left( \frac{(p+q)\pi n}{N} \right) \right],
$$

$$
= \frac{k_B T}{N} \gamma(t-t') \delta_{n\lambda} \frac{\delta_{pq}(1+\delta_{n0})}{2}.
$$

(S2)

B. The parameter $k_p$ relates to the variance of $X_p$

At thermal equilibrium via the preaveraging approximation, the memory effect of the friction coefficient vanishes, i.e., $\gamma(t-t') \to 2\gamma \cdot \delta(t-t')$. Then, Eq. 5 for $p \geq 1$ can be written as

$$
\dot{\gamma} X_p(t) = -k_p X_p(t) + \dot{g}_p(t),
$$

(S3)

where

$$
\langle \dot{g}_{pn}(t)\dot{g}_{q\lambda}(t') \rangle = \frac{\tilde{\gamma} k_B T}{N} \delta(t-t') \delta_{n\lambda} \delta_{pq}.
$$

(S4)

Since this Langevin equation for one degree of freedom corresponds to the Ornstein-Uhlenbeck process described by the stochastic differential equation [S4],

$$
dX_{pn}(t) = -\frac{k_p}{\gamma} X_{pn}(t) dt + \sqrt{\frac{k_B T}{N\gamma}} dB_t,
$$

(S5)

the variance of $X_p$ becomes

$$
\langle X_{pn}^2 \rangle_{CD} = \frac{k_B T/(N\gamma)}{2k_p/\tilde{\gamma}} = \frac{k_B T}{2Nk_p},
$$

(S6)

where $\langle \cdot \rangle_{CD}$ represents the average for all nucleosome beads within the chromatin domain (CD) at thermal equilibrium. Thus, this relation implies that the normal-coordinate amplitude satisfies the equipartition theorem at thermal equilibrium.
C. Asymptotic form of \( \langle X_p^2 \rangle_{CD} \)

Here, we omit the argument \( t \) to calculate the thermal average. Using integration by parts, the normal coordinates \( X_p \equiv \frac{1}{\pi} \int_0^N \cos \left( \frac{p \pi n}{N} \right) R(n) \, dn \) are rewritten as

\[
X_p = -\frac{1}{p\pi} \int_0^N \, \sin \left( \frac{p \pi n}{N} \right) \frac{\partial R(n)}{\partial n}. \tag{S7}
\]

Thus, \( \langle X_p^2 \rangle_{CD} \) is written as

\[
\langle X_p^2 \rangle_{CD} = \frac{1}{p^2 \pi^2} \int_0^N \, \sin \left( \frac{p \pi n}{N} \right) \sin \left( \frac{p \pi m}{N} \right) \frac{\partial^2}{\partial n \partial m} \langle |R(n) - R(m)|^2 \rangle_{CD}. \tag{S8}
\]

Using

\[
\frac{\partial R(n)}{\partial n} \cdot \frac{\partial R(m)}{\partial m} = -\frac{1}{2} \frac{\partial^2}{\partial n \partial m} [R(n) - R(m)]^2, \tag{S9}
\]

we can rewrite \( \langle X_p^2 \rangle_{CD} \) as

\[
\langle X_p^2 \rangle_{CD} = -\frac{1}{2p^2 \pi^2} \int_0^N \int_0^N \, \sin \left( \frac{p \pi n}{N} \right) \sin \left( \frac{p \pi m}{N} \right) \frac{\partial^2}{\partial n \partial m} \langle |R(n) - R(m)|^2 \rangle_{CD}. \tag{S10}
\]

Introducing a new variable \( l = m - n \) and substituting the size scaling (Eq. 4), we can make the following calculation:

\[
\langle X_p^2 \rangle_{CD} = \frac{1}{2p^2 \pi^2} \int_0^N \, \sin \left( \frac{p \pi n}{N} \right) \sin \left( \frac{p \pi (l + n)}{N} \right) \frac{\partial^2}{\partial l \partial n} \left( b_{\text{eff}}^2 |n - m|^{2/d_l} \right),
\]

\[
= \frac{b_{\text{eff}}^2}{2p^2 \pi^2} \frac{2}{d_l} \left( \frac{2}{d_l} - 1 \right) \int_0^N \sin \left( \frac{p \pi n}{N} \right) \sin \left( \frac{p \pi l}{N} \right) \int_{-n}^{N-n} dl \sin \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2} + \sin \left( \frac{p \pi n}{N} \right) \sin \left( \frac{p \pi l}{N} \right) \int_{-n}^{N-n} dl \cos \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2}. \tag{S11}
\]

The underlined integrals converge quickly to the following values if \( p \) is large:

\[
\int_{-n}^{N-n} dl \sin \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2} \approx \int_{-\infty}^{\infty} dl \sin \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2} = 0 \tag{S12}
\]

and

\[
\int_{-n}^{N-n} dl \cos \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2} \approx \int_{-\infty}^{\infty} dl \cos \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2}. \tag{S13}
\]

Therefore, we can obtain

\[
\langle X_p^2 \rangle_{CD} \approx \frac{b_{\text{eff}}^2}{2p^2 \pi^2} \frac{2}{d_l} \left( \frac{2}{d_l} - 1 \right) \frac{N}{2} \frac{2}{2} \int_0^\infty \cos \left( \frac{p \pi l}{N} \right) \left| l \right|^{2/d_l - 2}. \tag{S14}
\]

Using the formulas

\[
\int_0^\infty \cos(ax) x^{b-1} \, dx = \Gamma(b) \cos \left( \frac{\pi b}{2} \right) a^{-b} \quad \text{and} \quad z \Gamma(z) = \Gamma(z + 1), \tag{S15}
\]

we obtain

\[
\langle X_p^2 \rangle_{CD} \approx \frac{b_{\text{eff}}^2}{2p^2 \pi^2} \frac{2}{d_l} \left( \frac{2}{d_l} - 1 \right) \frac{N}{2} \frac{2}{2} \Gamma \left( \frac{3}{2} - \frac{2}{d_l} \right) \cos \left( \frac{\pi b}{2} \right) a^{-b}. \tag{S16}
\]
we can make the following formal calculations:

\[
\langle X_p^2 \rangle_{\text{CD}} \approx \frac{b_{\text{eff}}^2 N}{2p^2 \pi^2 d_t} \left( \frac{2}{d_t} - 1 \right) \Gamma(2/d_t - 1) \cos \left[ \frac{\pi}{2} \left( \frac{2}{d_t} - 1 \right) \right] \left( \frac{bN}{N} \right)^{1-2/d_t},
\]

\[
= \frac{b_{\text{eff}}^2 N^{2/d_t}}{2} \frac{2}{d_t} \Gamma(2/d_t) \cos \left( \frac{\pi}{d_t} - \frac{\pi}{2} \right) (pN)^{1-2/d_t},
\]

\[
= \frac{(R^2)_{\text{CD}}}{2} \Gamma(1 + 2/d_t) \sin(\pi/d_t) p^{-1-2/d_t},
\]

\[
= \frac{(R^2)_{\text{CD}}}{2A_{d_t}} p^{-1-2/d_t}, \quad (S16)
\]

where

\[
A_{d_t} = \frac{\pi^{1+2/d_t}}{\Gamma(1 + 2/d_t) \sin(\pi/d_t)} \quad (S17)
\]

is a dimensionless constant depending on the fractal dimension \(d_t\).

### D. The solution of Eq. 9

Performing the Laplace transform to Eq. 9, we obtain

\[
\tilde{\gamma}(s) \left[ s \tilde{C}_p(s) - C_p(0) \right] = -k_p \tilde{C}_p(s), \quad (S18)
\]

where \(\tilde{\gamma}(s)\) and \(\tilde{C}_p(s)\) are the Laplace transforms of the functions \(\gamma(t)\) and \(C_p(t)\), respectively. Since \(\gamma(t)\) is defined by Eq. 2, \(\tilde{\gamma}(s)\) is derived as follows:

\[
\tilde{\gamma}(s) = \frac{\gamma_\alpha}{\Gamma(1 - \alpha)} \int_0^\infty e^{-st} t^{-\alpha} dt,
\]

\[
= \frac{\gamma_\alpha}{\Gamma(1 - \alpha)} s^{\alpha-1} \int_0^\infty e^{-y} y^{(1-\alpha)-1} dy,
\]

\[
= \gamma_\alpha s^{\alpha-1}. \quad (S19)
\]

Therefore, \(\tilde{C}_p(s)\) is written as

\[
\tilde{C}_p(s) = C_p(0) \frac{\gamma_\alpha s^{\alpha-1}}{\gamma_\alpha s^{\alpha} + k_p} = C_p(0) \frac{s^{\alpha-1}}{s^{\alpha} + k_p/\gamma_\alpha}. \quad (S20)
\]

In addition, using the formula of the Laplace transform for the Mittag-Leffler function

\[
\mathcal{L} \left[ E_\alpha (-at^\alpha) \right](s) = \frac{s^{\alpha-1}}{s^{\alpha} + a}, \quad (S21)
\]

we can inversely find the solution

\[
C_p(t) = C_p(0) E_\alpha \left( -k_p/\gamma_\alpha \cdot t^\alpha \right). \quad (S22)
\]

By use of Eqs. 6 and 7,

\[
k_p = \frac{A_{d_t} \cdot 3k_B T}{N \gamma_\alpha (R^2)_{\text{CD}}} p^{1+2/d_t}. \quad (S23)
\]

Then, we can define the relaxation time

\[
\tau_{d_t,\alpha} \equiv \left( \frac{N \gamma_\alpha (R^2)_{\text{CD}}}{A_{d_t} \cdot 3k_B T} \right)^{1/\alpha}, \quad (S24)
\]

which has the physical dimension \(s\). If the initial condition reaches thermal equilibrium, \(C_p(0)\) becomes \(\langle X_p^2 \rangle_{\text{CD}}\). Thus, finally, we can derive the solution

\[
C_p(t) = \langle X_p^2 \rangle_{\text{CD}} E_\alpha \left[ -p^{1+2/d_t} (t/\tau_{d_t,\alpha})^\alpha \right]. \quad (S25)
\]
E. The MSD of the center of the CD

For $p = 0$, the normal coordinate $X_0(t)$ corresponds to the center of the CD,

$$R_G(t) = \frac{1}{N} \int^N R(n, t) \, dn.$$  \hfill (S26)

According to the Langevin equation (Eq. 5) and the FDR (Eq. S2) for $p = 0$, the motion obeys

$$\int^t_0 \gamma(t - t') \frac{dX_0(t')}{dt'} \, dt' = g_0(t), \quad \text{where} \quad \langle g_{0\alpha}(t) g_{0\lambda}(t') \rangle = \frac{k_B T}{N} \gamma(t - t') \delta_{\alpha\lambda}. \hfill (S27)$$

In general, for degree of freedom $x$ and velocity $v$, the MSD is associated with the velocity correlation as follows:

$$\langle \left[ x(t) - x(0) \right]^2 \rangle = \frac{1}{s^2} \mathcal{L} \left[ \langle v(0)v(t) \rangle \right] (s) = \frac{2}{s^2} \mathcal{C}_v(s). \hfill (S29)$$

Using the Laplace transform and the stationarity of the velocity correlation $C_v(t)$, this relation becomes more clear:

$$\mathcal{L} \left[ \left[ x(t) - x(0) \right]^2 \right] (s) = \frac{2}{s^2} \mathcal{L} \left[ \langle v(0)v(t) \rangle \right] (s) = \frac{2}{s^2} \mathcal{C}_v(s). \hfill (S29)$$

In terms of the fluctuation-dissipation theorem (FDT) [S2], we can derive the Laplace transform of the velocity correlation from the relationship between the average response and the FDR. The force balance between the average response of the system described by Eq. S27 and the external force $f(t)$ is written as

$$\int^t_0 \gamma(t - t') \langle v(t') \rangle \, dt' = f(t), \hfill (S30)$$

for one degree of freedom. The Laplace transform of this force balance equation becomes

$$\tilde{\gamma}(s) \langle \tilde{v}(s) \rangle = \tilde{f}(s). \hfill (S31)$$

Then, the ratio of the average velocity to the force, $\langle \tilde{v}(s) \rangle / \tilde{f}(s) = 1/\tilde{\gamma}(s)$, is called the complex admittance, and the FDT of the first kind represents the relationship between the complex admittance and the velocity correlation,

$$\frac{k_B T}{N} \frac{1}{\tilde{\gamma}(s)} = \tilde{C}_v(s), \hfill (S32)$$

where the coefficient $k_B T/N$ is caused by the FDT of the second kind for the system in Eq. S27.

Therefore, the Laplace transform of the MSD is written as

$$\mathcal{L} \left[ \left[ x(t) - x(0) \right]^2 \right] (s) = \frac{2}{s^2} \frac{k_B T}{N} \frac{1}{\tilde{\gamma}(s)} = \frac{2k_B T}{N\gamma_0} \frac{1}{s^{\alpha+1}}. \hfill (S33)$$
By use of the formula of the inverse Laplace transform, $L^{-1}[1/(s^{\alpha+1})](t) = t^{\alpha}/\Gamma(1+\alpha)$, the MSD can be obtained as

$$\langle (x(t) - x(0))^2 \rangle = \frac{2k_BT}{\Gamma(1+\alpha)N\gamma_\alpha} t^\alpha. \quad (S34)$$

Thus, the MSD of the center of the CD is derived as

$$\langle [X_0(t) - X_0(0)]^2 \rangle = 3 \frac{2k_BT}{\Gamma(1+\alpha)N\gamma_\alpha} t^\alpha,$$

$$= \frac{2\langle R^2 \rangle_{CD}}{A_{d_\ell}\Gamma(1+\alpha)} \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^\alpha. \quad (S35)$$

**F. The MSD for $t \ll \tau_{d_\ell,\alpha}$**

The MSD obtained in our experiment is calculated by averaging nucleosome movements at various positions in CDs. Then, we can replace the term $\cos^2 \left( \frac{\pi 2}{N} \right)$ in Eq. 8 by the average 1/2. Therefore, for $t \ll \tau_{d_\ell,\alpha}$, according to Eqs. 7 and 12, and the asymptotic form of the Mittag-Leffler function, $E_\alpha(-x) \approx \exp \left[ -x/\Gamma(1+\alpha) \right]$ for $x \ll 1$, the second term in the right hand side (RHS) of Eq. 8 can be expressed as

$$\text{MSD}(t) \approx 8 \sum_{p=1}^{\infty} \frac{\langle R^2 \rangle_{CD}}{2A_{d_\ell}} \frac{1}{p^{1+2/d_\ell}} \left\{ 1 - \exp \left[ - \frac{1}{\Gamma(1+\alpha)} \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^\alpha \right] \right\}. \quad (S36)$$

Converting the sum into the integral, the RHS becomes

$$\frac{2\langle R^2 \rangle_{CD}}{A_{d_\ell}} \int_0^\infty dp \frac{1}{p^{1+2/d_\ell}} \left[ 1 - e^{-t/(\tau_{d_\ell,\alpha})^\alpha/\Gamma(1+\alpha) p^{1+2/d_\ell}} \right]. \quad (S37)$$

Here, let us consider the integral formula calculated as follows:

$$\int_0^\infty dx \: x^{-1+a} \left( 1 - e^{-bx} \right) = \left[ \left( \frac{x-a}{a} \right) \left( e^{-bx} - 1 \right) \right]_0^\infty + \frac{bc}{a} \int_0^\infty dx \: x^{-a+1} e^{-bx},$$

$$= \frac{bc}{a} \int_0^\infty dy \: \left( \frac{y}{b} \right)^{1-a+1} e^{-y},$$

$$= \frac{b \varrho/c}{a} \int_0^\infty dy \: e^{-y} y^{(1-a)/c-1},$$

$$= \frac{b \varrho/c}{a} \Gamma(1-a/c). \quad (S38)$$

Therefore, the MSD for $t \ll \tau_{d_\ell,\alpha}$ can be written as

$$\text{MSD}(t) \approx \frac{2\langle R^2 \rangle_{CD}}{A_{d_\ell} \Gamma(1+\alpha)} \left[ \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^\alpha \right]^{2/(2+d_\ell)} \Gamma \left[ \frac{d_\ell}{2(2+d_\ell)} \right],$$

$$= \frac{2\langle R^2 \rangle_{CD}}{A_{d_\ell} \Gamma(1+\alpha)} \Gamma(1+\alpha) \frac{d_\ell}{2} \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^{-2/(2+d_\ell)} \Gamma \left[ \frac{d_\ell}{2(2+d_\ell)} \right] \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^{\alpha-2/(2+d_\ell)},$$

$$= \frac{2B_{d_\ell,\alpha} \langle R^2 \rangle_{CD}}{A_{d_\ell} \Gamma(1+\alpha)} \left( \frac{t}{\tau_{d_\ell,\alpha}} \right)^{-\alpha+2/(2+d_\ell)}, \quad (S39)$$

where

$$B_{d_\ell,\alpha} = \frac{d_\ell}{2} \Gamma(1+\alpha)^{d_\ell/(2+d_\ell)} \Gamma \left[ \frac{d_\ell}{2(2+d_\ell)} \right]$$

is a dimensionless constant depending on $d_\ell$ and $\alpha$. 
II. REMARKS ON THE HYDRODYNAMIC EFFECT FOR OUR POLYMER MODEL

In describing the Langevin equation of polymers with the hydrodynamic interaction, the interaction affects the mobility matrix [S1, S5]. This situation corresponds to an ideal case where hydrodynamic interactions are not screened. Calculating the effect of the mobility matrix for the normal coordinates $X_p(t)$ under the preaveraging approximation, $k_p$ in Eq. 5 is changed into $\bar{k}_p$ with the following $p$-dependence:

$$\bar{k}_p \sim k_p \cdot p^{1/d-1} \sim p^{3/d}. \quad (S41)$$

Therefore, when we calculate the MSD as above, we need to calculate the integral

$$\int_0^\infty dp \frac{1}{p^{1+2/d}} \left[ 1 - e^{-\left(t/\tau\right)\alpha}/\Gamma(1+\alpha) p^{3/d} \right]. \quad (S42)$$

By use of the integral formula (Eq. S38), the scaling of the MSD for $t \ll \tau$ can be written as

$$\text{MSD}(t) \sim t^{\alpha - 2/3}. \quad (S43)$$

This means that the hydrodynamic interaction cancels out the effect of the size scaling described by the fractal dimension $d_f$, and that the exponent of the MSD depends on only the exponent $\alpha$, which relates to the memory effect of the viscoelastic medium.