Supplement S4: Casp3-induced Degradation of XIAP Does not Result in Bistability

Experimental evidence suggests that Casp3 activation may result in XIAP cleavage and/or degradation, although this seems to be a cell-type-specific phenomenon (see Discussion). In the following, we demonstrate that Casp3-induced XIAP degradation (‘inhibition of inhibition’ = positive circuit) does not result in physiologically relevant bistability in the absence of other feedback amplification loops.

Figure S4: Model of Casp3-induced XIAP Degradation

In order to obtain analytical results, we first focussed on a simplified model of Casp3-induced XIAP degradation, which comprises only the black reactions in Fig. S4. The corresponding differential equations read:

\[
\frac{dC_3}{dt} = k_1 - (k_2 + k_3) \cdot C_3 \\
\frac{dC_3^*}{dt} = k_3 \cdot C_3 - (k_4 + k_5 \cdot X) \cdot C_3^* + k_6 \cdot C_3^* \cdot X \\
\frac{dC_3^* \cdot X}{dt} = k_5 \cdot X \cdot C_3^* - (k_7 + k_8) \cdot C_3^* \cdot X \\
\frac{dX}{dt} = k_7 + k_5 \cdot C_3^* \cdot X - \left( k_7 \cdot C_3^* + k_8 + k_6 \cdot C_3^* \right) \cdot X
\]

The steady state condition of active Casp3 (\(dC_3^*/dt = 0\)) can be written as a quadratic equation in \(C_3^*\), which implies that the steady state of \(C_3^*\) cannot be bistable.

We next numerically analyzed a more realistic model (black and grey arrows in Fig. S4), where XIAP inhibits both Casp3 and Casp9. Here, the feedback loops discussed in the paper (i.e., Casp3-mediated feedback cleavage of Casp9 and XIAP-mediated feedback) were assumed to be inactive in order to focus on the role of Casp3-mediated XIAP degradation. Hence, XIAP was assumed to bind to Casp3 and Casp9 in a non-competitive manner.
All kinetic parameters were chosen according to Tables 1 (see main text) and S1 (see Supplement S1; with $\alpha = 1$). Additionally, Casp3-mediated XIAP degradation (reaction 9 in Fig. S4) was modelled as an irreversible second-order process with the rate constant $k_9 = 3 \times 10^{6}\text{M}^{-1}\text{s}^{-1}$, which is the value measured for high-affinity substrates of Casp3 [1,2].

These studies revealed that Casp3-induced XIAP degradation does not result in bistability for experimentally measured protein concentrations (Casp3 = 200 nM; Casp9 = 20 nM; XIAP = 40 nM). Although some bistability could be observed for significantly different expression levels (e.g., for XIAP > 100 nM), hysteresis was restricted to a very small stimulus range, so that the stimulus-response was virtually indistinguishable from that of a monostable system. Importantly, the physiological feedback strength (i.e., $k_9$ in Fig. S4) is likely to be lower than that we assumed here, as most Casp3 substrates do not match the optimal Casp3 target sequence, DEVD [1]. For example, Casp3 cleaves XIAP at a suboptimal site [3]. Likewise, Akt, a protein kinase that mediates XIAP stabilization unless it is processed and thereby inactivated by Casp3 [4], also does not contain the optimal DEVD-target sequence [5]. As high feedback strength is required for bistability [6], we can conclude that Casp3-induced XIAP degradation does not result in physiologically relevant bistability as long as other feedback amplification loops are absent.

REFERENCES: