Supporting Information for
MEDYAN: Mechanochemical Simulations of Contraction and Polarity Alignment in Actomyosin Networks

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Model details.

A) Chemical model details.

Simulation space is divided into discrete compartments, with the Kuramoto length chosen in a similar manner as recent work [1]. We do not consider mechanical interactions between diffusing chemical species, or their exact positions within the compartments. The compartment size is fixed throughout the simulation. The polymers in the system do not move or slip in the simulation space unless acted on by an external force, which is controlled by the potentials outlined in the Mechanical Model. All reactions are chosen and controlled by the Gillespie algorithm [2, 3]. Diffusion (and other forms of transport), polymerization, capping, and branching nucleation reactions occur as in previous work [1,4–7]. The chemical reactions new to the MEDYAN model are outlined below:

- If we denote L and M as cross-linker and motor species, respectively, the binding and unbinding reactions can be described as follows:

\[ P_1 + P_2 + L \leftrightarrow P_1LP_2, \text{ and} \]
\[ P_1 + P_2 + M \leftrightarrow P_1MP_2, \]  

where \( P_1 \) and \( P_2 \) are both polymers. Both equations [1] and [2] assume that the polymers are within the reaction range of this cross-linker or motor species.

- A motor can walk along either polymer it is bound to with the following form:

\[ M_n \leftrightarrow M_{n+1}, \]  

where \( n \) denotes the binding site on the polymer. This implicitly assumes that the next binding site to move to on the polymer is not occupied. The rates of these reactions can be affected by external stresses, which is described in S3 Text.
• A non-branching filament nucleation reaction can occur in the bulk where two monomer species bind to form a new polymer. This reaction can occur with the following form:

\[ X_1 + X_2 \rightarrow P, \]  

(4)

where \( X_1 \) and \( X_2 \) are any diffusing species in the system. This creates a new polymer \( P \) with chemical composition \( X_1X_2 \). Nucleated polymers are placed randomly in the simulation space corresponding to the compartment location of their reactant monomers.

• Polymers can also be severed implicitly with the following form:

\[ P_0 \rightarrow P_1 + P_2, \]  

(5)

where \( P_1 \) and \( P_2 \) denote the polymers resulting from a split of polymer \( P_0 \). This reaction keeps in tact the chemical composition of the original polymer.

• In the case of actin filaments, monomers can undergo an aging reaction corresponding to the steps of F-actin ATP hydrolysis. This reaction takes the form:

\[ X_{1,f} \rightarrow X_{2,f}, \]  

(6)

where \( X_{1,f} \) and \( X_{2,f} \) represent two distinct chemical species in the filament.

B) Mechanical effects of various chemical reactions.

Most chemical reactions have distinct mechanical effects on the network. We outline the chemical reactions and their mechanical effect below:

• Polymerization and depolymerization can occur at either end of a polymer. When a polymerization event occurs, the equilibrium length \( l_0 \) will increase by a monomer size, denoted by \( l_{\text{mon}} \). When \( l_0 \) has reached its maximum size, which we will denote by \( l_{\text{cyl}} \), this cylinder stops growing and a new cylinder with \( l_0 = l_{\text{mon}} \) is created. Similarly, when a depolymerization event occurs, \( l_0 \) will decrease by \( l_{\text{mon}} \), and when \( l_0 = l_{\text{mon}} \), the cylinder will be removed.

• Motor and cross-linker binding can occur on neighboring polymers. When a binding reaction occurs, the respective interaction is created between the two binding cylinders as outlined in the Mechanical Model. The positions \( \alpha \) and \( \beta \) are determined stochastically at binding. When unbinding, the interaction is removed from the two cylinders.

• Motor walking can occur on a polymer. When a walking reaction occurs, the positional parameter \( \alpha \) (or \( \beta \), depending on which side of the motor is walking) will increase by some discrete value. The motor may change cylinders due to a walking reaction, which would effectively reset the positional parameter and move the motor onto the next cylinder in the polymer chain. This movement will in turn generate a stress in the motor, and will eventually be equilibrated.
Branching nucleation can occur on a polymer. When a branching nucleation reaction occurs, a new cylinder with $l_0 = l_{\text{mon}}$ is created at a branching site on the mother cylinder, which is determined stochastically. The respective interaction is created between the two cylinders as outlined in the Mechanical Model. This branched cylinder can now polymerize or depolymerize normally at its leading end. When branch unbinding occurs, this interaction is removed between the two cylinders, effectively freeing the daughter polymer.

C) Mechanical minimization details.

Mechanical equilibration is performed with any choice of force fields (which are outlined in the Mechanical Model) after a number of chemical reaction steps. Mechanical equilibration is performed using a conjugate gradient energy minimization algorithm. The system can be minimized to any force minimization tolerance $g_{\text{tolerance}}$. Depending on the size and nature of the active network being simulated, $g_{\text{tolerance}}$ as well as the timestep per mechanical equilibration, denoted as $t_{\text{minimize}}$, can be chosen accordingly. For examples of choosing these parameters for a simulated active network, see S2 Text, which describes choosing a reasonable $g_{\text{tolerance}}$ and $t_{\text{minimize}}$ for the example actomyosin systems presented in the paper.

D) Software implementation

The MEDYAN model has been implemented in a serial C++ code which uses efficient data structures and object-oriented programming paradigms to simulate active networks with the scheme described in earlier sections. Fig. shows the implemented software’s general workflow. Upon reading user input regarding chemical species and reactions, mechanical interactions, and mechanochemical feedback relationships of constituent elements defined in the system, as well as various simulation parameters and algorithm specifications for these interactions in a number of system input files, the simulation system is constructed with all necessary data structures needed for the updating and management of key simulation components. By allowing a flexible creation of simulation elements, interactions, and algorithms, this software implementation of the MEDYAN model is able to perform simulations for a range of active matter systems with customizable components under various user-defined conditions. Additionally, this software has been constructed in highly compartmentalized fashion such that modifications and additions to the individual mechanical and chemical components, including interactions as well as algorithms, can be easily implemented.

After the system is initialized with the above components, the system controller object, which acts as the simulation driver, is responsible for evolving the system in time via chemical and mechanical interaction controllers. These child controllers, which also are initialized using user-defined parameters and are responsible for executing the specified simulation algorithms for stochastic reaction-diffusion and mechanical equilibration, then iteratively evolve the simulation system in time. The time evolution and subsequent deformations and growth of the simulated network, including the addition or deletion of components and other interactions that may affect the structure of the network, are then updated in the system by the main controller using an efficient callback system. In this way, chemical reactions, as well as mechanical interactions and deformations, can efficiently update system elements only when needed.

This software package, including source code for the serial C++ MEDYAN implementation, documentation on usage and compilation, and a trajectory visualization tool, is publicly available for general scientific use (www.medyan.org). It is encouraged that users create new patches to the
Figure 1: **A workflow diagram describing the MEDYAN software implementation.** (1) User input is given to create the (2) simulation system, which involves (3) setting up the necessary structures (4) and initializing the system controllers. During a simulation, (2-4) constantly communicate via an efficient callback system. We note that many less essential elements of the simulation workflow are omitted from this diagram.

existing code, tailoring it for many scientific purposes. In future work, this implementation will be made to run on parallel architectures, using some of the many available C++ parallelization tools, including the OpenMP and MPI libraries.

**References**


