

Supporting Text S1

A Disorder Induced Domino-Like Destabilization Mechanism Governs the Folding and Functional Dynamics of the Repeat Protein I κ B α

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The Wako-Saitô-Muñoz-Eaton (WSME) model

The free-energy of a particular microstate (m, n) (i.e., a string of 1's between and including m and n) in the WSME model with electrostatics and solvation free-energy [19,21] is given by

$$\Delta F = \sum \Delta G_{m,n}^{stab} - T \sum_m^n \Delta S_{conf} \quad (\text{S.1})$$

The stabilization free-energy of a microstate (first term in the above equation) is represented as a sum of van der Waals interactions (E_{vdW}), electrostatic potential (E_{elec}) and solvation free-energy (ΔG_{solv}) arising from purely native contributions:

$$\Delta G_{m,n}^{stab} = E_{vdW} + E_{elec} + \Delta G_{solv} \quad (\text{S.2})$$

The second term corresponds to the entropic cost of fixing residues to the native conformation at the temperature T . The interacting partners that contribute to the van der Waals energy are identified by setting a distance cut-off (r_{cut}) to the pair-wise heavy-atom partners (i, j) calculated from the PDB file.

$$E_{vdW} = \sum_{m,n} \xi_{i,j} \rho \quad (\text{S.3})$$

where $\rho = 1$ if $r_{ij} \leq r_{cut}$ and $\rho = 0$ otherwise. In atomic-level force-fields the interaction energies are distance dependent but since the WSME model pre-assumes an ensemble derived from the native structure a distance dependent energy is not required. The r_{cut} was fixed to 6 Å and nearest neighbors were excluded from the contact calculation as before[19,21].

A Debye-Hückel (DH) treatment is employed for the electrostatic potential term:

$$E_{elec} = \sum_{m,n} K_{Coulomb} \frac{q_i q_j}{\epsilon_{eff} r_{ij}} \exp(-r_{ij} \kappa) \quad (\text{S.4})$$

wherein $K_{Coulomb}$ is the Coulomb constant (1389 kJ.Å/mol), q_i is the charge on the atom i , r_{ij} is the distance between charge centers i and j , and ϵ_{eff} is the effective dielectric constant and is fixed to 29. $1/\kappa$ is the Debye screening length that depends on ϵ_{eff} , solvent ionic-strength (I) and temperature (T) as

$$\kappa^2 = \frac{8\pi e^2 I}{\epsilon_{eff} k_B T} \quad (S.5)$$

where k_B is the Boltzmann's constant, and e is the elementary charge. Charges were assigned to atoms according to pH 7.0 protonation state and I was fixed to the experimental value of 0.05 M[10].

The solvation free-energy is approximated as being proportional to the number of formed contacts ($x_{cont}^{m,n}$) in that microstate with the proportionality constant being ΔC_p^{cont} , which is the temperature-independent heat capacity change upon fixing a native contact. Therefore,

$$\Delta G_{solv} = x_{cont}^{m,n} \Delta C_p^{cont} \left[(T - T_{ref}) - T \ln(T/T_{ref}) \right] \quad (S.6)$$

where T_{ref} is the reference temperature which is fixed to 385 K[34]. A uniform conformational entropy cost (ΔS_{conf}) is assigned to residues independent of sequence or native secondary-structure.

The partition function (Z) is calculated employing the transfer-matrix formalism of Wako and Saitô[16,17]:

$$Z(T) = v_l \left[\prod_{i=1}^N X_i \right] v_r^tr \quad (S.7)$$

where

$$X_i = \begin{pmatrix} 1 & 1 & 1 & \cdots & 1 & 1 \\ z & 0 & 0 & \cdots & & 0 \\ 0 & H_1^{(i)}z & 0 & & & \vdots \\ & & H_2^{(i)}z & & 0 & 0 \\ & 0 & & & H_{N-2}^{(i)}z & H_{N-1}^{(i)}z \end{pmatrix}$$

$$v_l = (1, 1, 1, \dots, 1)$$

$$v_r = (1, 0, 0, \dots, 0)$$

and

$$H_k^{(i)} = \exp\left(-\beta \sum_{j=1}^k \Delta G^{stab}\right) \quad (k \leq N-i) \quad (\text{S.8})$$

$$H_k^{(i)} = 0 \quad (k > N-i)$$

Here, $\beta = 1/RT$ and $z = \exp(\Delta S_{conf}/R)$ where R is $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$. The one-dimensional free-energy profiles are constructed by accumulating the total statistical weight for members of the ensemble with different number of structured residues.

The overall probability of a particular residue to be folded (p_f^i) can be obtained from

$$p_f^i = Z^{-1} v_l \left[\prod_{j=1}^{i-1} X_j \right] \left[\frac{\partial X_i}{\partial \ln z} \right] \left[\prod_{j=i+1}^N X_j \right] v_r^{tr} \quad (\text{S.9})$$

The final parameters from fit to the excess heat capacity profile are: $\Delta S_{conf} = -18.1 \text{ J mol}^{-1} \text{ K}^{-1}$, $\varepsilon = -70.1 \text{ J mol}^{-1}$ while ΔC_p^{cont} is fixed to $-0.358 \text{ J mol}^{-1} \text{ K}^{-1}$ [19].

Chemical Denaturation

Chemical denaturation effects are introduced by a phenomenological constant that decreases the stabilization free-energy linearly with denaturant concentration ($[D]$):

$$\Delta G_{m,n}^{stab}([D]) = E_{vdW} + E_{elec} + \Delta G_{solv} - x_{cont}^{m,n} m^{cont} [D] \quad (\text{S.10})$$

Other parameters including entropic cost were fixed to the original values extracted from the characterization of temperature-induced denaturation.